### **Brain Networks**

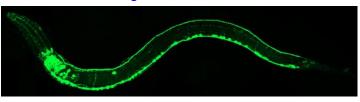
Ed Bullmore

Cambridge Complex Networks Network 27<sup>th</sup> September 2011

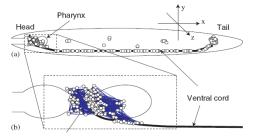
### The small world of the worm's brain



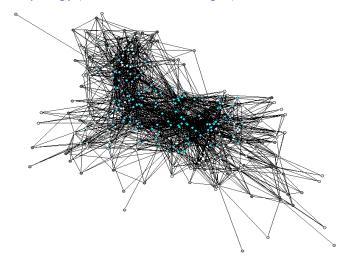
#### Caenorhabditis elegans



#### Anatomy (277 neurons, 7000 synapses)



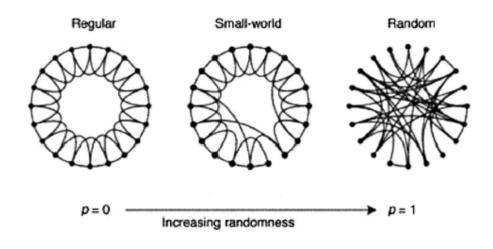
#### Topology (277 nodes, 7000 edges)

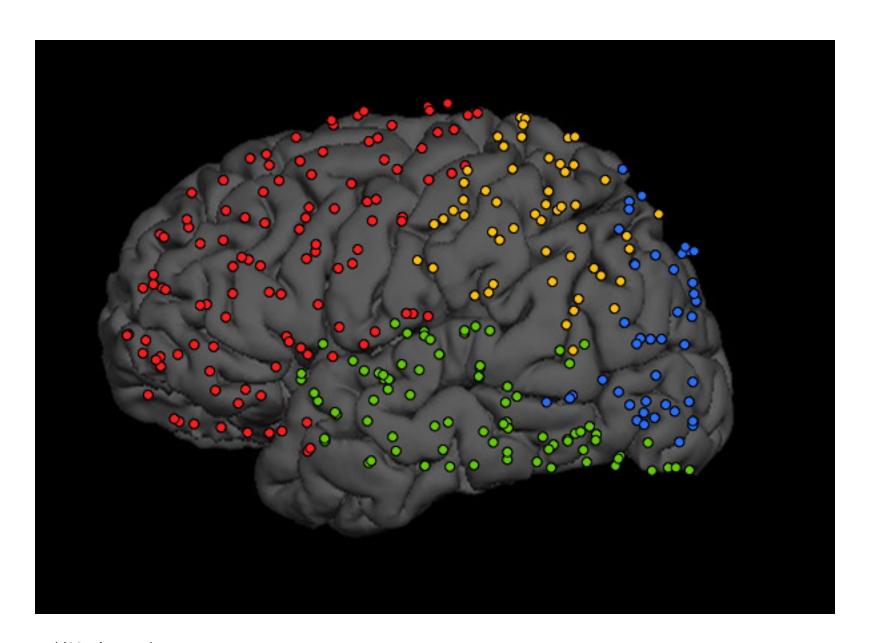


#### Small-world

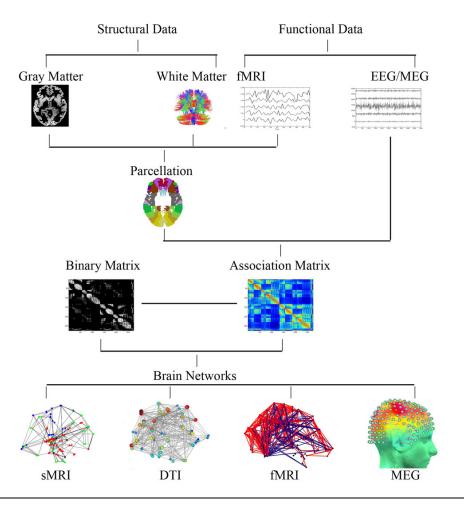
- High clustering or cliquishness of connections between neighboring nodes
- Short path length or high efficiency of communication between any pair of nodes
- Cost-efficient
  - 40% maximum efficiency of information transfer for only 4% maximum connection cost

Watts & Strogatz (1998) Nature; Latora & Marchiori (2001) Phys Rev Lett





### From neuroimaging to brain graphs



- Estimate an association matrix from the data
  - What are the nodes?
  - What metric of connectivity?
- 2. Generate an adjacency matrix from the association matrix
  - What are the edges?
- Measure topological properties of each graph
- 4. Make comparisons between graphs

Brain graphs are statistical models entailing assumptions and trade-offs which influence parameter values

Brain graph parameters make sense relativistically, not absolutely; comparison between graphs is not trivial

## Many network properties are conserved across many scales and kinds and species of brain graphs

### **Small worldness**

- high clustering
- short path length or high efficiency

### **Cost-efficiency**

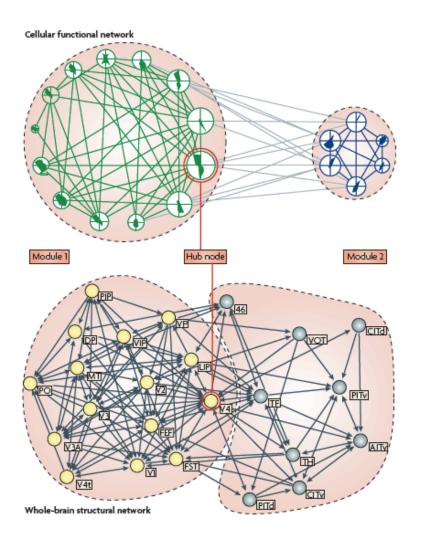
 high efficiency of information transfer for relatively low connection cost

### **Hub nodes**

fat-tailed degree distributions

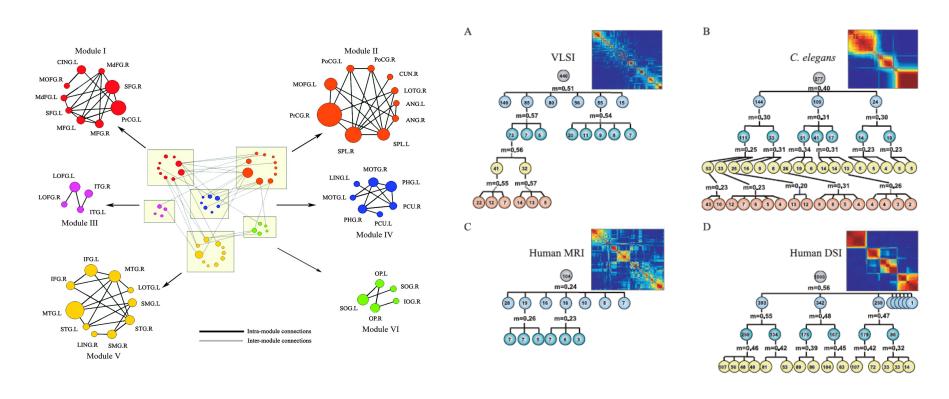
### **Modularity**

 nodes are more densely connected to other nodes in the same module than to nodes in other modules



Bullmore & Sporns (2009) Nat Rev Neurosci

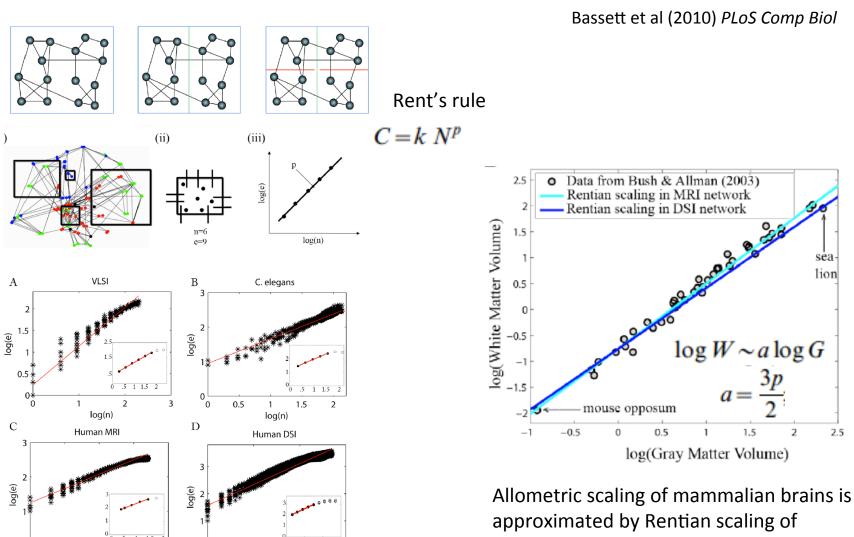
## Human brain graphs and other information processing networks are hierarchically modular



Nodes in the same module are often, but not always, anatomical as well as topological neighbours: so intra-modular edges will be shorter distance than inter-modular edges

Brain graphs typically have modules within modules

### Rentian and allometric scaling in brains



1.5

log(n)

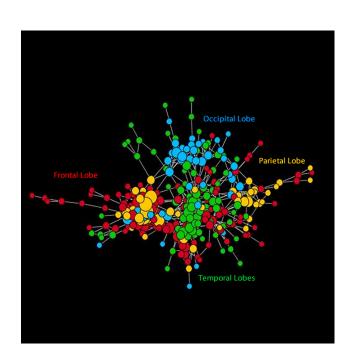
2

log(n)

0.5

human brain

## What's special and what's universal about human brains compared to other information networks?

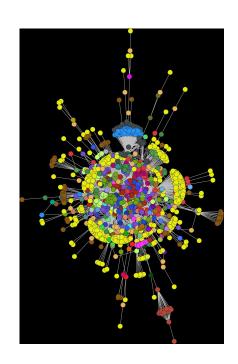


Utilities

Consumer, non-clinical

Healthcare

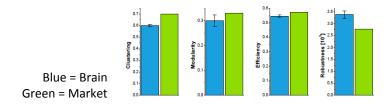
Technology



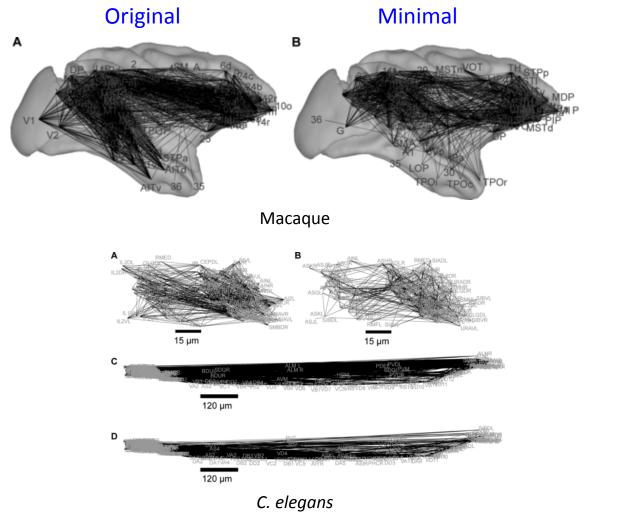
Human Brain Network Resting state FMRI

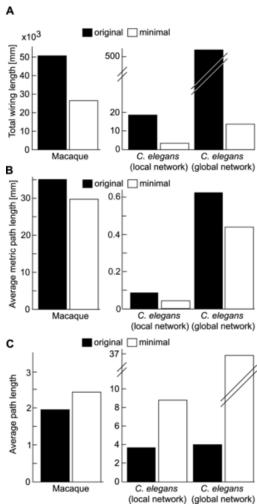
Economic Network
New York Stock Exchange

Social Network
Twitter #gadaffi

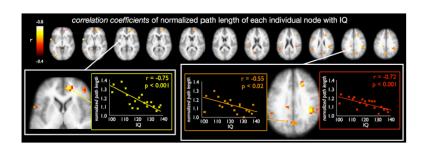


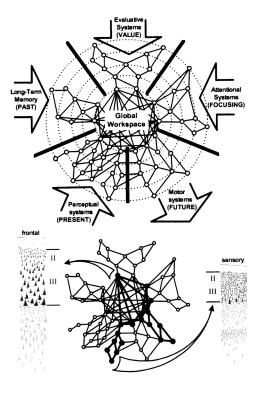
## Brain networks are economically wired but do *not* strictly minimise wiring cost





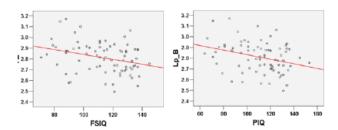
# Expensive, long-range integrative connections may be "worth it" for extra cognitive capacity





Greater efficiency (or shorter path length)
 of human brain networks is correlated with
 higher IQ

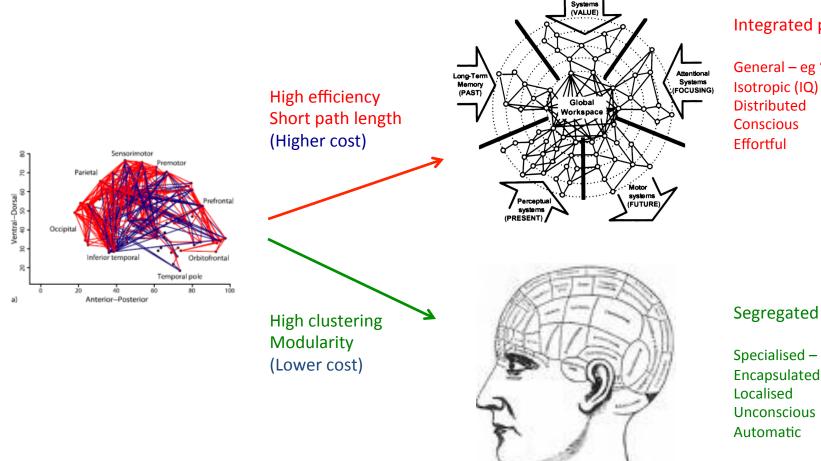
Van den Heuvel et al (2009) *J Neurosci*; Li et al (2009) *PLoS Comp Biol*; Bassett et al (2010) *PLos Comp Biol*;



 Global (neuronal) workspace theory predicts integrative networks will be required for conscious, effortful processing

Dehaene et al (1998) *Proc Natl Acad Sci*Baars (1993) *A cognitive theory of consciousness* 

### Cartoon interpretation of economical small-world architecture in terms of cognitive processes



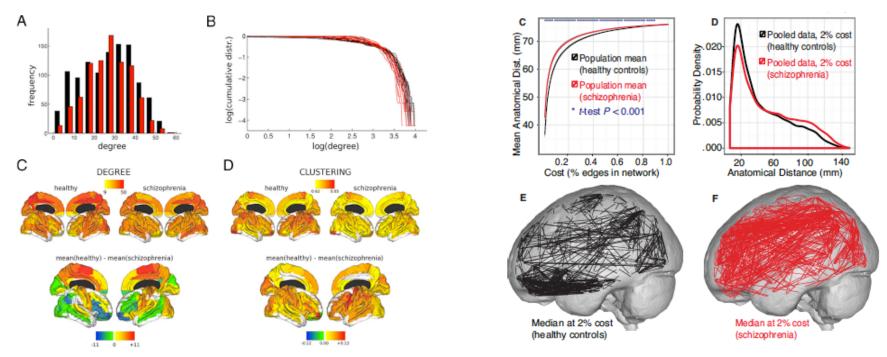
#### Integrated processes

General – eg "executive"

### Segregated processes

Specialised – eg face vision

## Disordered brain development may involve an abnormal trade-off between network cost and topology

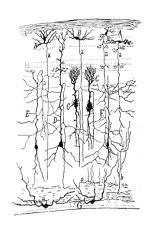


schizophrenia connectomes

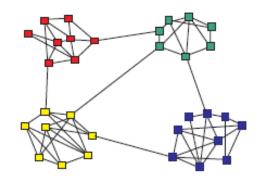
Topologically - less clustered, less modular and less hub-dominated: "subtle randomization"

Anatomically – less economically connected, a higher proportion of long distance edges

Lynall et al (2010) *J Neurosci*; Alexander-Bloch et al (2010) *Frontiers Sys Neurosci*; Rubinov et al (2009) *Hum Brain Mapp* 



### Conclusions



- About 200 years ago we began to understand the anatomical organization of brain networks; in the last 10 years or so we have also begun to understand the topological properties of brain networks
- Graph theoretical analysis is a way of simplifying complex systems that is generalizable to topological analysis of many scales and kinds of data and may provide a useful mathematical framework for modeling the connectome
- Hypothetically, brain networks "negotiate a trade-off" between minimization of connection costs and maximization of behaviourally advantageous topological properties, like efficiency
- Recent data suggest that cost-efficiency trade-offs in brain networks
  - are heritable
  - are renegotiated dynamically in response to changing cognitive demands (msec)
  - are relevant to normal and abnormal brain development (years)
  - can be modulated by drugs affecting cognitive performance